# A Novel Modulation Scheme for Isolated PWM Active-Clamp Ćuk DC/DC Converter 

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#### Abstract

A novel modulation scheme for a bidirectional isolated pulsewidth modulation active-clamp (PAC)-Ćuk converter is presented in this article. In the PAC-Cuk converter, the clamping circuit consisting of a capacitor, a series inductor, and an active device enables zero-voltage-switching (ZVS) turn-ON capability of all the active devices. This additional circuit equips the converter with three independent control parameters. This article discusses power transfer, ZVS region, and circulating current dependency on the control parameters across the converter gain. Minimal circulating current is generally desired to decrease the conduction losses. With the help of the proposed modulation technique, the optimization of the control parameters to achieve lower circulating current while ensuring ZVS operation is also discussed. A $2-\mathrm{kW}$ experimental converter is also designed and fabricated to validate the analysis.


Index Terms-Active clamp, circulating current optimization, Ćuk converter, de/dc converter, zero-voltage switching (ZVS).

## NOMENCLATURE

$V_{\text {in }}, V_{o} \quad$ Steady-state average input and output voltages
$I_{L \text { in }}, I_{L o}$
$L_{\text {in }}, L_{o}$
$S_{P 1}, S_{P 2}$
$S_{S 1}, S_{S 2}$
$T_{\text {sw }}$
$d_{1}, d_{2}$
$\Delta_{\phi}$
$\Delta_{\phi} \quad$ Phase-shift ratio defined as the ratio between the time period when both main switches $S_{P 1}$ and $S_{S 1}$ are inactive in the switching period, $T_{\text {sw }}$.

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$\left.\left.\begin{array}{ll}d_{1}^{\prime}, d_{2}^{\prime} & \begin{array}{l}\text { Duty cycles of the primary-side auxiliary switch } \\ \left(S_{P 2}\right) \text { and the secondary-side auxiliary switch }\end{array} \\ \left(S_{S 2}\right), \text { which is complementary of the main } \\ \text { switch. }\end{array}\right\} \begin{array}{l}\text { Primary- and secondary-side blocking capaci- } \\ \text { tors, respectively. }\end{array}\right\}$

## I. Introduction

BIDIRECTIONAL dc/dc converters have emerged as the center of research in power electronics. The capability of bidirectional power flow allows this category of converters to
be used in a multitude of applications, such as dc smart grids [1]-[3], electric vehicles [4], [5], and energy storage systems [6]-[8]. Extensive research work has focused on the development of reliable, compact, and efficient isolated dc/dc converters. Conventional galvanic isolation for these systems requires bulky and costly low-frequency transformers [9], [10]. An isolated $\mathrm{dc} / \mathrm{dc}$ converter is equipped with high-frequency-transformerbased isolation, yielding a cheaper and lightweight isolation solution. High-voltage conversion gain required in some applications can also be realized by using the turns ratio of the transformer [11], [12].

Numerous isolated bidirectional dc/dc converters have been proposed and researched in recent times. The most popular among them is the dual active bridge ( DAB ), introduced in [13]. The converter requires two H -bridges, comprising a total of eight active switches for bidirectional power flow. The single-phaseshift (SPS) modulation has a limited zero-voltage-switching (ZVS) region of operation and suffers from higher current stress [14]. Other modulation techniques are proposed, such as those based on dual phase shift (DPS) [15], triple phase shift (TPS) [16], and others with some variations [17]. These modulation techniques extend the ZVS turn-ON region and decrease the circulating current, resulting in higher efficiency of the system. However, circulating current minimization requires complex computation. Also, the DAB dc/dc converter has discontinuous input and output currents and, hence, requires additional filtering for practical applications. An additional blocking capacitor or control technique is also required to block the dc magnetization of the HF transformer.

In contrast, an isolated Ćuk converter requires only two active switches [18] to realize the bidirectional dc/dc converter. In addition, the input and output inductors of the pulsewidth modulation (PWM)-clamp Ćuk converter ensure continuous current flow, reducing the filter size. The magnetic component of the isolated Ćuk converter can also be integrated, resulting in a high-density system [19], [20]. However, switches in a conventional Ćuk converter are hard-switched, resulting in higher losses. In a bidirectional isolated Ćuk converter, the leakage inductance of a typical high-frequency transformer requires a lossy snubber circuit to dissipate the energy stored in the leakage inductor to limit the drain-to-source voltage across the devices [21]. This causes additional losses in the converter, reducing its application. Li et al. [22] explored a lossless active-snubber solution for bidirectional application. However, the snubber requires a complicated circuit with additional switches, diodes, capacitors, and inductors. The diodes incur additional losses, yielding a limited improvement in efficiency.

Incorporating an active-clamp snubber circuit in an isolated Ćuk converter can also limit the voltage stress on the components and transfer energy from the leakage inductance of the transformer [23]-[25] to auxiliary capacitors of the active-clamp circuit. The stored energy is then redirected back to the system with the possibility to achieve ZVS on the main switches and the added auxiliary switches.

The PWM active-clamp (PAC) circuit introduced in [26] enables the converter to achieve ZVS turn-ON. The active-clamp circuit exhibits circulating current, which results in the ZVS


Fig. 1. Proposed bidirectional PAC-Ćuk converter topology.
turn-ON of the main switch. In [25] and [27], a PAC circuit has been applied to a Ćuk converter for unidirectional power flow.

In [24], a high-switching-frequency-operated bidirectional PAC-Ćuk converter was introduced. However, the ZVS operation of the converter relies on the magnetizing inductance of the transformer, whereas the active-clamp circuit is used as a snubber circuit to mitigate the effect of transformer leakage inductance. The magnetizing current of the transformer needs to be larger than the sum of input and output inductors for the ZVS operation, resulting in twice the current stress on the components. In addition, lower leakage inductance requires a larger auxiliary and blocking capacitor to avoid resonance between them, and hence, it is not practical for low-switching-frequency operation.

Fig 1. shows the proposed isolated bidirectional PAC-Ćuk converter. Two active-clamp circuits are added to the conventional isolated Ćuk converter: The primary-side circuit comprises capacitor $C_{T 1}$ and switch $S_{P 2}$, whereas the secondaryside circuit comprises capacitor $C_{T 2}$ and switch $S_{S 2}$. An additional series inductor $L_{r}$ is also added, which is common to both active-clamp circuits. Two active clamp circuits are required in the proposed converter for a bidirectional operation. The PAC-Ćuk converter enables ZVS turn-ON of the switches while increasing the switch count by two and requires additional auxiliary capacitors. The leakage inductance energy of the transformer is now used by the clamp circuit to circulate current, which assists in ZVS turn-ON. As in the case of the conventional isolated Ćuk converter, the input and output inductors of the PAC-Ćuk converter provide continuous current flow. The proposed modulation of the bidirectional PAC-Ćuk converter is based on three control parameters as shown in Fig 1: the duty cycle of $S_{P 1}, d_{1}$; the duty cycle of $S_{S 1}, d_{2}$; and the phase-shift ratio $\Delta_{\phi}$, defined as the ratio between the time period when both $S_{P 1}$ and $S_{S 1}$ are inactive in the switching period. Table I provides a comparison between the PAC-Ćuk converter and other competitive converters and their modulation techniques. The proposed modulation for the PAC-Ćuk converter is easier to implement, has a wide ZVS range, and yields competitive efficiency for wide gain.

In conventional modulation [23]-[25], [27], the duty cycles of $S_{P 1}$ and $S_{S 1}$ are complimentary, whereas for the proposed modulation, the duty cycles are controlled independently. Independent control of the two duties and the phase-shift ratio allows three degrees of freedom for modulation. A more

TABLE I
Comparison Between the PAC-Cúk and the DC-DC Converters

| Converter | Soft-switching <br> range | Soft-switching and optimization <br> complexities | Range of <br> converter gain, G | Power range | Efficiency |
| :---: | :---: | :---: | :---: | :---: | :---: |
| DAB with SPS [28] | Narrow | Low | $0.6-1.2$ | 200 W to 1 kW | $85.0-96.1 \%$ |
| DAB with DPS [29] | Medium | Medium | $0.4-1$ | 380 W |  |
| DAB with TPS [28] | Wide | High | $75.0-95.0 \%$ |  |  |
| DAB with unified TPS [16] | Wide | High | $0.6-1.2$ | 200 W to 1 kW | $96.0-97.3 \%$ |
| CLLC [4] | Wide | High | $300-900 \mathrm{~W}$ | $95.0-97.0 \%$ |  |
| PAC-Cuk with the proposed | Wide | Low | 1 | 200 W to 1 kW | $95.5-97.4 \%$ |
| modulation |  | $0.6-1.3$ | 400 W to 2 kW | $96.5-97.8 \%$ |  |

accurate closed-form model as a function of the three independent control parameters of the PAC-Ćuk converter is developed in this article with experimental verification to form a new modulation scheme. The effects of the three control parameters on the power transfer capability of the converter, its ZVS region, and the circulating current through the leakage inductor are analyzed in detail using the model. Higher degrees of freedom enable the PAC-Ćuk converter to provide a set of solutions for the same operating condition, which allows the possibility of multiobjective optimization. In this article, the objective of the optimization is to minimize circulating current for a given output power while ensuring ZVS operation to limit conduction losses. Optimization of the duty cycles $d_{1}$ and $d_{2}$ to achieve the minimal circulating current for a constant $\Delta_{\phi}$ is presented in this article.

The rest of this article is organized as follows. Section II presents the operation and analysis of the proposed converter. In Section III, power transfer, circulating current, and ZVS range are discussed. Section IV provides hardware design considerations and optimization of the control parameters for minimal circulating current. Section V provides the experimental results for validation of the analysis. Finally, Section VI concludes this article.

## II. Operation and Analysis of the PAC-Ćuk Converter

The PAC-Ćuk converter offers ZVS turn-ON of all the switches by using active-clamp circuits and the equivalent series inductor $L_{\text {eq }}$. The active-clamp circuit forces negative drain-to-source current, $i_{\mathrm{ds}}$, through the FET forcing the body diode to turn ON before the gate, resulting in ZVS turn-ON of the switches. Large auxiliary capacitors ( $C_{T 1}$ and $C_{T 2}$ ) and blocking capacitors $\left(C_{B 1}\right.$ and $\left.C_{B 2}\right)$ act as a constant voltage $(\mathrm{CV})$ source over a switching cycle. These capacitor voltages are imposed on the equivalent series inductor $L_{\mathrm{eq}}$ as per the active state of switches $\left(S_{P 1}, S_{P 2}, S_{S 1}, S_{S 2}\right)$, resulting in power transfer and circulating current. Linear operation of the converter and analysis requires that the inductor current $i_{\text {Leq }}$ must be linear across the main modes, which is ensured by avoiding $L C$ resonance during the operational modes. The minimum capacitor size condition is discussed in Section IV. In this article, only the forward power flow is considered where $\Delta_{\phi}$ is referred from turn-OFF of $S_{P 1}$ to turn-ON of $S_{S 1}$. For backward power flow, $\Delta_{\phi}$ is referred from turn-OFF of $S_{S 1}$ to turn-ON of $S_{P 1}$. The backward power flow follows the same analysis due to converter symmetry and is not
discussed in detail. The transformer turn ratio of unity is chosen for simplicity in this article.

The operation of the converter can be divided into eight modes: four main modes $\left(M_{1}, M_{2}, M_{3}\right.$, and $\left.M_{4}\right)$ and four transition modes $\left(T_{1}, T_{2}, T_{3}\right.$, and $\left.T_{4}\right)$ as shown in Fig. 2. The waveforms associated with the modes are shown in Fig. 3. By applying volt-second balance on input inductor $L_{\text {in }}$, output inductor $L_{o}$, and series inductor $L_{\text {eq }}$ over a switching cycle, the following steady-state average voltages are obtained:

$$
\begin{align*}
V_{C T 1} & =V_{\mathrm{in}} / d_{1}^{\prime}  \tag{1}\\
V_{C T 2} & =V_{o} / d_{2}^{\prime}  \tag{2}\\
V_{C B 1}+V_{C B 2} & =V_{\mathrm{in}}+V_{o .} . \tag{3}
\end{align*}
$$

The duration of the phase shift between the primary and secondary gate signals is $\Delta_{\phi} T_{\mathrm{sw}}$, as shown in Fig. 3. The input inductor ripple ( $\Delta I_{L \text { in }}$ ) and output inductor current ripple $\left(\Delta I_{L o}\right)$ are given as follows:

$$
\begin{align*}
\Delta I_{L \mathrm{in}} & =\frac{V_{\mathrm{in}} d_{1} T_{\mathrm{sw}}}{2 L_{\mathrm{in}}}  \tag{4}\\
\Delta I_{L o} & =\frac{V_{o} d_{2} T_{\mathrm{sw}}}{2 L_{o}} \tag{5}
\end{align*}
$$

In Sections II and III, the current flowing into the node with voltage $v_{1}(t)$ is defined as $i_{1}(t)$, whereas the current coming out of the node with voltage $v_{2}(t)$ is defined as $i_{2}(t)$, as shown in Fig. 2. Currents $i_{1}(t)$ and $i_{2}(t)$ can be defined as follows:

$$
\begin{align*}
& i_{1}(t)=i_{L \mathrm{in}}(t)-i_{L \mathrm{eq}}(t)  \tag{6}\\
& i_{2}(t)=i_{L o}(t)+i_{\text {Leq }}(t) . \tag{7}
\end{align*}
$$

## A. Modes of Operation of the Bidirectional PAC-Ćuk Converter

Analysis of modes of operation for the bidirectional PAC-Ćuk converter is drawn using Figs. 2 and 3. At $t_{0}, S_{P 2}$ and $S_{S 2}$ are conducting. Drain-to-source current of switch $S_{P 2}, i_{P 2}(t)$, is equal to $-i_{1}(t)$ and is negative in amplitude.

Mode $1\left[t_{0}<t<t_{1}\right]$ (Main mode, $M_{1}$ ): In this main mode, gate of $S_{P 2}$ is still OFF. As $i_{P 2}(t)$ is negative, the body diode of $S_{P 2}$ is conducting. Before $i_{P 2}(t)$ becomes positive, the gate is applied on $S_{P 2}$, resulting in ZVS turn-ON of the device. Since the switches $S_{P 2}$ and $S_{S 2}$ are active, the voltage across the


Mode $2\left[t_{1}-t_{2}\right]$ : Transition mode $\mathrm{T}_{1}$


Mode $4\left[t_{3}-t_{4}\right]$ : Transition mode $\mathrm{T}_{2}$


Mode $5\left[t_{4}-t_{5}\right]:$ Main mode $\mathrm{M}_{3}$


Mode $6\left[t_{5}-t_{6}\right]$ : Transition mode $\mathrm{T}_{3}$


Mode $7\left[t_{6}-t_{7}\right]$ : Main mode $\mathrm{M}_{4}$


Mode $8\left[t_{7}-t_{0}\right]$ : Transition mode $\mathrm{T}_{4}$
Fig. 2. Modes of forward operation of the bidirectional PAC-Ćuk converter.
inductor $L_{\mathrm{eq}}$ equals $V_{C T 1}+V_{C T 2}-V_{C B 1}-V_{C B 2}$. Current $i_{\text {Leq }}(t)$ ramps up linearly and is given as follows:
$i_{L e q}(t)=\frac{V_{C T 1}+V_{C T 2}-V_{C B 1}-V_{C B 2}}{L_{\mathrm{eq}}}\left(t-t_{0}\right)+i_{L e q}\left(t_{0}\right)$.


Fig. 3. Operating waveform of the proposed PAC-Ćuk converter.

At time $t_{1}$, mode $M_{1}$ ends with the removal of gate of $S_{S 2}$. Duration of this mode, $T_{M 1}$ is given as follows:

$$
\begin{equation*}
T_{M 1}=t_{1}-t_{0}=\Delta_{\phi} T_{\mathrm{sw}}-\left(T_{T 1}+T_{T 4}\right) / 2 \tag{9}
\end{equation*}
$$

where $T_{T 1}$ and $T_{T 4}$ are the durations of the transition modes $T_{2}$ and $T_{4}$, respectively.

Mode 2 [ $t_{1}<t<t_{2}$ ](Transition mode, $T_{1}$ ): In this transition mode, $T_{1}, S_{S 2}$ is turned OFF by removing the gate signal. TurnOFF of $S_{S 2}$ results in current $i_{2}(t)$ to divert from $S_{S 2}$ to $S_{S 1}$, resulting in discharging of the output capacitance of $S_{S 1}, C_{\mathrm{oss}, S 1}$, and charging of the output capacitance of $S_{S 2}, C_{\mathrm{oss}, S 2}$. ZVS turn-ON of $S_{S 1}$ requires that the $C_{\text {oss }, S 1}$ is fully discharged [equivalent to $v_{2}(t)$ falling to zero] before the gate of $S_{S 1}$ is applied. Current $i_{2}(t)$ results in $v_{2}(t)$ to fall linearly until it is
clamped by the body diode of $S_{S 1}$ marking the end of this mode. The duration of the transition mode $T_{T 1}$ is given as follows:

$$
\begin{align*}
T_{T 1}=t_{2}-t_{1} & =\frac{\left(C_{\mathrm{oss}, S 1}+C_{\mathrm{oss}, S 2}\right) V_{C T 2}}{i_{2}\left(t_{1}\right)}  \tag{10}\\
i_{2}\left(t_{1}\right) & =\left(I_{L o}+\Delta I_{L o}\right)+i_{L \mathrm{eq}}\left(t_{1}\right) \tag{11}
\end{align*}
$$

where inductor current $i_{\text {Leq }}\left(t_{1}\right)$ is given by (8).
Mode 3 [ $t_{2}<t<t_{3}$ ] (Main mode, $M_{2}$ ): At time $t_{2}$, the body diode of $S_{S 1}$ is conducting as $i_{S 1}(t)$, equal to $-i_{2}(t)$, is negative. The gate is applied to $S_{S 1}$ while $i_{S 1}(t)$ is still negative, resulting in the turn-ON of $S_{S 1}$ under ZVS. As $S_{P 2}$ is also active, the voltage across the inductor $L_{\text {eq }}$ is now reduced to $V_{C T 1}-$ $V_{C B 1}-V_{C B 2}$, which, depending on $V_{C T 1}$, can be positive or negative. The series inductor current $i_{L \text { eq }}(t)$ is given as follows:

$$
\begin{equation*}
i_{L \mathrm{eq}}(t)=\frac{V_{C T 1}-V_{C B 1}-V_{C B 2}}{L_{\mathrm{eq}}}\left(t-t_{2}\right)+i_{L \mathrm{eq}}\left(t_{2}\right) . \tag{12}
\end{equation*}
$$

During this mode, current $i_{P 2}(t)$ equals $-i_{1}(t)$, whereas $i_{S 1}$ equals $-i_{2}(t)$. The duration of this mode $T_{M 2}$ is given as follows:

$$
\begin{equation*}
T_{M 2}=t_{3}-t_{2}=\left(d_{1}^{\prime}-\Delta_{\phi}\right) T_{\mathrm{sw}}-\left(T_{T 2}+T_{T 1}\right) / 2 \tag{13}
\end{equation*}
$$

where $T_{T 2}$ and $T_{T 1}$ are the durations of the transition modes $T_{2}$ and $T_{1}$, respectively.

Mode $4\left[t_{3}<t<t_{4}\right]$ (Transition mode, $T_{2}$ ): At time $t_{3}$, duty cycle of $S_{P 2},\left(1-d_{1}\right)$, is elapsed and $S_{P 2}$ is turned OFF by removing the gate signal. Current $i_{1}(t)$ starts to discharge $C_{\mathrm{oss}, P 1}$ and charge $C_{\mathrm{oss}, P 2}$. The voltage $v_{1}(t)$ falls linearly due to current $i_{1}(t)$ until it reaches zero and gets clamped by the body diode of $S_{P 1}$, marking the end of this mode. The duration of this transition mode, $T_{T 2}$, and current $i_{1}\left(t_{3}\right)$ is given as follows:

$$
\begin{align*}
T_{T 2}=t_{4}-t_{3} & =\frac{\left(C_{\mathrm{oss}, P 1}+C_{\mathrm{oss}, P 2}\right) V_{C T 1}}{i_{1}\left(t_{3}\right)}  \tag{14}\\
i_{1}\left(t_{3}\right) & =\left(I_{L \mathrm{in}}+\Delta I_{L \text { in }}\right)-i_{L \mathrm{eq}}\left(t_{3}\right) \tag{15}
\end{align*}
$$

where $i_{\text {Leq }}\left(t_{3}\right)$ is obtained using (12).
Mode $5\left[t_{4}<t<t_{5}\right]$ (Main mode, $M_{3}$ ): At time $t_{4}$, the body diode of $S_{P 1}$ is still conducting as current $i_{P 1}(t)$, equal to $i_{1}(t)$, is still negative. Applying the gate on $S_{P 1}$ results in ZVS turn-ON of $S_{P 1}$. As $S_{P 1}$ and $S_{S 1}$ are ON, the voltage across the inductor $L_{\mathrm{eq}}$ is equal to $-V_{C B 1}-V_{C B 2}$. The negative voltage results in fall of the inductor current $i_{\text {Leq }}(t)$ as shown in Fig. 3 and is given as follows:

$$
\begin{equation*}
i_{L \mathrm{eq}}(t)=\frac{-V_{C B 1}-V_{C B 2}}{L_{\mathrm{eq}}}\left(t-t_{4}\right)+i_{L \mathrm{eq}}\left(t_{4}\right) . \tag{16}
\end{equation*}
$$

The duration of this mode, $T_{M 3}$, is given as follows:

$$
\begin{equation*}
T_{M 3}=t_{5}-t_{4}=\left(d_{1}-d_{2}^{\prime}+\Delta_{\phi}\right) T_{\mathrm{sw}}-\left(T_{T 3}+T_{T 2}\right) / 2 \tag{17}
\end{equation*}
$$

where $T_{T 3}$ and $T_{T 2}$ are the durations of the transition modes $T_{3}$ and $T_{2}$, respectively.

Mode $6\left[t_{5}<t<t_{6}\right.$ ] (Transition mode, $T_{3}$ ): Current $i_{\text {Leq }}(t)$ forces the current $i_{2}(t)$ to become negative. At time $t_{5}, S_{S 1}$ is turned OFF by removing the gate signal. Current $i_{2}(t)$ starts to discharge capacitance $C_{\mathrm{oss}, S 1}$ and charge $C_{\mathrm{oss}, S 2}$. The voltage
$v_{2}(t)$ rises linearly until it reaches $V_{C T 2}$ and gets clamped by the body diode of $S_{S 2}$. The duration of this transition mode $T_{T 3}$ and current $i_{2}\left(t_{5}\right)$ is given as follows:

$$
\begin{align*}
T_{T 3}=t_{6}-t_{5} & =\frac{\left(C_{\mathrm{oss}, S 1}+C_{\mathrm{oss}, S 2}\right) V_{C T 2}}{-i_{2}\left(t_{5}\right)}  \tag{18}\\
i_{2}\left(t_{5}\right) & =\left(I_{L o}+\Delta I_{L o}\right)+i_{L \mathrm{eq}}\left(t_{5}\right) \tag{19}
\end{align*}
$$

where $i_{\text {Leq }}\left(t_{5}\right)$ is obtained using (16).
Mode 7 [ $t_{6}<t<t_{7}$ ] (Main mode, $M_{4}$ ): As $C_{\text {oss }, S 2}$ is fully discharged, the diode of $S_{S 2}$ starts to conduct at time instant $t_{6}$. While current $i_{S 2}(t)$, equal to $i_{2}(t)$, is still negative, applying the gate on $S 2$ results in ZVS turn-ON of $S_{S 2}$. With $S_{P 1}$ and $S_{S 2}$ ON, the voltage across the series inductor $L_{\text {eq }}$ is equal to $V_{C T 2}-V_{C B 1}-V_{C B 2}$. Current $i_{L \text { eq }}(t)$ rises or falls in this mode according to the voltage across the inductor $L_{\text {eq }}$ and is given as follows:

$$
\begin{equation*}
i_{L \mathrm{eq}}(t)=\frac{V_{C T 2}-V_{C B 1}-V_{C B 2}}{L_{\mathrm{eq}}}\left(t-t_{6}\right)+i_{L \mathrm{eq}}\left(t_{6}\right) \tag{20}
\end{equation*}
$$

The duration of this main mode, $T_{M 4}$, is given as follows:

$$
\begin{equation*}
T_{M 4}=t_{7}-t_{6}=\left(d_{2}^{\prime}-\Delta_{\phi}\right) T_{\mathrm{sw}}-\left(T_{T 4}+T_{T 3}\right) / 2 \tag{21}
\end{equation*}
$$

where $T_{T 4}$ and $T_{T 3}$ are the durations of the transition modes $T_{4}$ and $T_{3}$, respectively.

Mode $8\left[t_{7}<t<t_{0}+T_{s w}\right]$ (Transition mode, $T_{4}$ ): At time $t_{7}, S_{P 1}$ is turned OFF by removing the gate signal. Current $i_{1}(t)$ starts to discharge the capacitance $C_{\mathrm{oss}, P 2}$ and charge $C_{\mathrm{oss}, P 1}$. The voltage $v_{1}(t)$ rises linearly till it reaches $V_{C T 1}$ and clamped by body diode of $S_{P 2}$. The duration of this transition mode, $T_{T 4}$, and current $i_{1}\left(t_{7}\right)$ is given as follows:

$$
\begin{align*}
T_{T 4} & =t_{0}+T_{\mathrm{sw}}-t_{7}=\frac{\left(C_{\mathrm{oss}, P 1}+C_{\mathrm{oss}, P 2}\right) V_{C T 1}}{-i_{2}\left(t_{7}\right)}  \tag{22}\\
i_{1}\left(t_{7}\right) & =\left(I_{L \mathrm{in}}+\Delta I_{L \mathrm{in}}\right)-i_{L \mathrm{eq}}\left(t_{7}\right) \tag{23}
\end{align*}
$$

where $i_{L \mathrm{eq}}\left(t_{7}\right)$ is obtained using (20).

## III. Power Transfer, Circulating Current, and ZVS ANALYSIS

In a conventional Ćuk converter, the energy is transferred from the input to the output through the blocking capacitor. In the PAC-Ćuk converter, energy is transferred via the blocking capacitor and the series inductor. The PAC-Ćuk converter has additional modes (Modes $M_{1}$ and $M_{3}$ ) where the ON and OFF states of the main switches $S_{P 1}$ and $S_{S 1}$ overlap, resulting in high $d i / d t$ limited only by the series inductor. More accurate analysis requires accounting for these overlapped modes. Also, the input and output inductor currents in the PAC-Ćuk converter are confined through either $S_{P 1}$ and $S_{S 1}$ or $C_{T 1}$ and $C_{T 2}$, respectively, and should be considered in the converter analysis. Current $i_{L \mathrm{eq}}(t)$ is dependent upon the voltage of the capacitors, $V_{C T 1}, V_{C T 2}, V_{C B 1}$, and $V_{C B 2}$, as given by (8), (12), (16), and (20).

Power transfer, circulating current, and ZVS analysis, which are essential for the analysis of this topology, require series inductor current states. The transition modes $\left(T_{1}, T_{2}, T_{3}\right.$, and $\left.T_{4}\right)$


Fig. 4. Simplified model of the proposed PAC-Ćuk converter for power and circulating current analysis. (a) Primary referred circuit. (b) AC equivalent of the circuit shown in (a). (c) Waveforms associated with the circuit.
are active for an insignificant time compared to the main modes ( $M_{1}, M_{2}, M_{3}$, and $M_{4}$ ) and can be ignored in power flow and circulating current analysis. Hence, the topology is reduced to four main modes of operation, as shown Fig. 4(c). A simplified circuit is developed as depicted in Fig. 4(a) to analyze the power transfer and circulating current through the series inductor. Node voltage $v_{2}(t)$ referred to the primary side is denoted by $v_{2}^{\prime}(t)$ for the unity gain transformer. $C_{B}$ is the lumped blocking capacitor equivalent of series connected $C_{B 1}$ and $C_{B 2}$. The effect of transformer magnetizing inductance $L_{m}$ is ignored in the simplified circuit as magnetizing current is insignificant for $L_{m} \gg L_{\text {eq }}$.

Node voltages $v_{1}(t)$ and $v_{2}^{\prime}(t)$ are imposed on $L_{\text {eq }}$ and $C_{B}$ as shown in Fig. 4(a). DC components of $v_{1}(t)$ and $v_{2}^{\prime}(t)$ are $V_{\text {in }}$ and $-V_{o}$, respectively, and are blocked by $C_{B}$. Fig. 4(b) shows the ac equivalent of the circuit shown in Fig. 4(a), which is obtained by removing the dc components of $v_{1}(t)$ and $v_{2}^{\prime}(t)$. Applying the gyrator theory [9], [10], an equivalent circuit is formed by placing separate inductors $L_{\text {eq }}$ across the two voltage sources to determine $i_{\text {Leq }}(t) . v_{1, \text { ac }}(t)$ and $v_{2, \text { ac }}^{\prime}(t)$ produce $i_{\text {Leq }, 1}(t)$ and $i_{\text {Leq, } 2}(t)$, respectively, as shown in Fig. 4(b) and (c), where $i_{L e q}(t)=i_{L e q, 1}(t)-i_{L e q, 2}(t) . v_{1, \text { ac }}(t)$ and $v_{2, \text { ac }}^{\prime}(t)$ for the four main modes are given as follows:

$$
\begin{align*}
& v_{1, \mathrm{ac}}(t)=\left\{\begin{array}{lll}
V_{C T 1} d_{1} & \text { when } t_{0} \leq t<t_{1} & {\left[M_{1}\right]} \\
V_{C T 1} d_{1} & \text { when } t_{1} \leq t<t_{2} & {\left[M_{2}\right]} \\
-V_{C T 1} d_{1}^{\prime} & \text { when } t_{2} \leq t<t_{3} & {\left[M_{3}\right]} \\
-V_{C T 1} d_{1}^{\prime} & \text { when } t_{3} \leq t<t_{0}+T_{\mathrm{sw}}\left[M_{4}\right]
\end{array}\right.  \tag{24}\\
& v_{2^{\prime}, \mathrm{ac}}(t)=\left\{\begin{array}{lll}
-V_{C T 2} d_{2}^{\prime} & \text { when } t_{0} \leq t<t_{1} & {\left[M_{1}\right]} \\
V_{C T 2} d_{2} & \text { when } t_{1} \leq t<t_{2} & {\left[M_{2}\right]} \\
V_{C T 2} d_{2} & \text { when } t_{2} \leq t<t_{3} & {\left[M_{3}\right]} \\
-V_{C T 2} d_{2}^{\prime} & \text { when } t_{3} \leq t<t_{0}+T_{\mathrm{sw}} & {\left[M_{4}\right]}
\end{array}\right. \tag{25}
\end{align*}
$$

where $d_{1}^{\prime}=1-d_{1}$ and $d_{2}^{\prime}=1-d_{2}$.

## A. Power Transfer Analysis

The output power of the PAC-Ćuk converter is equivalent to the total power transferred to $v_{2}^{\prime}(t)$ by $i_{L \text { eq }}(t)$ and is given as follows:

$$
\begin{align*}
P_{o}= & \frac{1}{T_{\mathrm{sw}}} \int_{0}^{T_{\mathrm{sw}}} v_{2}^{\prime}(t) i_{L \mathrm{eq}}(t) d t=\frac{1}{T_{\mathrm{sw}}} \int_{0}^{T_{\mathrm{sw}}} \\
& \times\left(V_{2, \mathrm{dc}}^{\prime} i_{L \mathrm{eq}}(t)+v_{2, \mathrm{ac}}^{\prime}(t) i_{L \mathrm{eq}}(t)\right) d t \tag{26}
\end{align*}
$$

where $V_{2, \mathrm{dc}}^{\prime}$ is the dc component, and $v_{2, \mathrm{ac}}^{\prime}(t)$ is the ac component of $v_{2}^{\prime}(t)$. As the average of $i_{\text {Leq }}(t)=0$ over a switching cycle, power transferred through the dc component is zero. Simplifying (26) results in the following:

$$
\begin{align*}
P_{o} & =\frac{1}{T_{\mathrm{sw}}} \int_{0}^{T_{\mathrm{sw}}} v_{2, \mathrm{ac}}^{\prime}(t)\left(i_{L \mathrm{eq}, 1}(t)-i_{L \mathrm{eq}, 2}(t)\right) d t \\
& =\frac{1}{T_{\mathrm{sw}}} \int_{0}^{T_{\mathrm{sw}}} v_{2, \mathrm{ac}}^{\prime}(t) i_{L \mathrm{eq}, 1}(t) d t \tag{27}
\end{align*}
$$

From (27), it can be noted that the power transferred to $v_{2}^{\prime}(t)$ is linked to the current produced by $v_{1}(t)$ that flows through $L_{\text {eq }}$. Hence, the powers transferred within each main mode ( $M_{1}, M_{2}, M_{3}$, and $M_{4}$ ) are obtained as follows:

$$
\begin{align*}
& P_{1}=\frac{V_{C T 1} V_{C T 2} d_{1} d_{2} T_{\mathrm{sw}}}{2 L_{\mathrm{eq}}} \Delta_{\phi}\left(d_{1}^{\prime}-\Delta_{\phi}\right)  \tag{28a}\\
& P_{2}=\frac{V_{C T 1} V_{C T 2} d_{1} d^{\prime} T_{\mathrm{sw}}}{2 L_{\mathrm{eq}}} \Delta_{\phi}\left(d_{1}^{\prime}-\Delta_{\phi}\right)  \tag{28b}\\
& P_{3}=\frac{V_{C T 1} V_{C T 2} d_{1}^{\prime} d^{\prime}{ }_{2} T_{\mathrm{sw}}}{2 L_{\mathrm{eq}}}\left(d_{2}^{\prime}-\Delta_{\phi}\right)\left(d_{2}-d_{1}+\Delta_{\phi}\right) \tag{28c}
\end{align*}
$$



Fig. 5. Three-dimensional plot showing power transfer dependency on duty cycles $\left(d_{1}\right.$ and $\left.d_{2}\right)$ for $V_{\text {in }}=350 \mathrm{~V}, V_{o}=350 \mathrm{~V}, L_{\text {eq }}=200 \mu \mathrm{H}$, and $\Delta_{\phi}=0.05$.

$$
\begin{equation*}
P_{4}=\frac{V_{C T 1} V_{C T 2} d_{1}^{\prime} d_{2} T_{\mathrm{sw}}}{2 L_{\mathrm{eq}}}\left(d_{2}^{\prime}-\Delta_{\phi}\right)\left(d_{2}-d_{1}+\Delta_{\phi}\right) . \tag{28d}
\end{equation*}
$$

Using the above-mentioned power equations and substituting the capacitor voltage relationship from (1) and (2), total power transferred in a steady state over a switching cycle is given as follows:

$$
\begin{equation*}
P_{o}=\frac{V_{\mathrm{in}} V_{o} T_{\mathrm{sw}}}{2 L_{\mathrm{eq}}}\left(2 \Delta_{\phi}+\left(d_{1}+d_{2}-1\right)-\frac{\Delta_{\phi}^{2}}{d_{1}^{\prime} d_{2}^{\prime}}\right) \tag{29}
\end{equation*}
$$

The power transferred during the transition modes is ignored as the duration of the transition modes is small compared to the main modes. It can be observed from (29) that the power transferred is linearly dependent upon the three control parameters . For a resistive load, the gain of the converter is obtained by substituting $P_{o}=V_{o}^{2} / R_{L}$. In a conventional Ćuk converter, the duty cycle of the main switches is complementary ( $d_{1}=1-d_{2}$ ). If conventional modulation of the Ćuk converter is implemented, the power transfer will be only the function of phase-shit ratio, $\Delta_{\phi}$. Fig. 5 shows a 3-D plot of power transferred to the output as a function of control parameters $\left(d_{1}\right.$ and $\left.d_{2}\right)$ for a constant $\Delta_{\phi}$. Fig. 7(d)-(f) shows the impact of $\Delta_{\phi}$ on the power transfer. Power transfer given by (29) is also valid for backward power flow by referring to the power and $\Delta_{\phi}$ from the secondary side.

## B. Circulating Current Analysis

In the PAC-Ćuk converter, ZVS turn-ON of all the switches requires circulating current through the inductor, $L_{\text {eq }}$. High circulating current results in higher conduction loss and, hence, should be limited while ensuring ZVS. One method to quantify the circulating current is by taking the mean square of $i_{L e q}(t)$


Fig. 6. Three-dimensional plot showing mean square series inductor current per Watt $\left(I_{L, \mathrm{RMS}}^{2} / \mathrm{W}\right)$ dependancy on duty cycles $\left(d_{1}\right.$ and $\left.d_{2}\right)$ for $V_{\text {in }}=350 \mathrm{~V}$, $V_{o}=350 \mathrm{~V}, L_{\text {eq }}=200 \mu \mathrm{H}$, and phase-shift ratio $\Delta_{\phi}=0.05$.
over a switching cycle denoted by $I_{L, \text { RMS }}^{2}$. Parasitic resistive elements present in the path of current $i_{L \text { eq }}(t)$ result in the conduction loss proportional to $I_{L, \mathrm{RMS}}^{2} \cdot I_{L, \mathrm{RMS}}^{2}$ can be computed by taking the mean square inductor current in each main mode and is given as follows:

$$
\begin{equation*}
I_{L, \mathrm{RMS}}^{2}=\frac{1}{T_{\mathrm{sw}}} \sum_{i=1}^{4} \int_{t_{i-1}}^{t_{i}} i_{L \mathrm{eq}}^{2}(t) d t \tag{30}
\end{equation*}
$$

where $i$ is the index of the main mode, $M_{i}$.
Inductor current, $i_{\text {Leq }}(t)$, is calculated using the ac equivalent circuit shown in Fig. 4. As $i_{\text {Leq }}(t)$ is linear for each main mode, it can be described as follows:

$$
\begin{equation*}
i_{L e q}(t)=m_{i}\left(t-t_{i-1}\right)+i_{L e q}\left(t_{i-1}\right) \tag{31}
\end{equation*}
$$

where $m_{i}$ is the slope of the current, $i_{\text {Leq }}\left(t_{i-1}\right)$ is the initial condition of the current at the start of the $i$ th mode. Slope $m_{i}$ and initial condition $i_{\text {Leq }}\left(t_{i-1}\right)$ are obtained using $i_{L e q, 1}(t)$ and $i_{\text {Leq }, 2}(t)$ as shown in Fig. 4(c) and are summarized in Table II.

The total mean square current $I_{L, \text { RMS }}^{2}$ over a switching cycle is obtained by using (30) and is given by (32) shown at the bottom of this page. In Fig. 6, $I_{L, \text { RMS }}^{2}$ normalized by power transferred is shown to provide better insight into the circulating current relation with the duty cycles $d_{1}$ and $d_{2}$ for constant phase-shift, $\Delta_{\phi}$. It can be seen from the figure that $I_{L, \text { RMS }}^{2}$ per unit power transferred takes a convex shape; hence, the minimum current for the required output power is found by the optimization of $d_{1}, d_{2}$, and $\Delta_{\phi}$. Fig. 7(d)-(f) shows the impact of $\Delta_{\phi}$ on the circulating current. Increasing $\Delta_{\phi}$ results in higher circulating current compared with $d_{1}$ and $d_{2}$ for high $\Delta_{\phi}$.

$$
\begin{align*}
I_{L, \mathrm{RMS}}^{2}= & \left(\frac{T_{\mathrm{sw}}}{L_{\mathrm{eq}}}\right)^{2}\left\{\frac{V_{o}\left(12 V_{\mathrm{in}} \Delta_{\phi}^{2}+V_{o}\right)}{12}+\frac{V_{\mathrm{in}} d_{1}^{2}\left(V_{\mathrm{in}}+4 V_{o}\right)}{12}+\frac{V_{\mathrm{in}} d_{2}^{\prime 2}\left(4 V_{\mathrm{in}}+V_{o}\right)}{12}\right. \\
& \left.-\frac{V_{o} d_{2}^{\prime}\left(V_{o}+6 V_{\mathrm{in}} \Delta_{\phi}\right)}{6}-\frac{V_{\mathrm{in}} V_{o} \Delta_{\phi}^{3}}{3 d_{2}^{\prime}-3 d_{1} d_{2}^{\prime}}-\frac{V_{\mathrm{in}} V_{o} d_{1}\left(3 d_{2}^{\prime}-6 \Delta_{\phi}+1\right)}{6}\right\} . \tag{32}
\end{align*}
$$



Fig. 7. Plots to depict dependency of power transfer, circulating current, and ZVS region of the PAC-Cuk converter on different system parameters. All graphs have $d_{1}$ on the $x$-axis and $d_{2}$ on the $y$-axis. (a)-(f) Contour plots with both power transfer and mean square current per unit power along with the ZVS region for different operating conditions.

TABLE II
Series Inductor Current Equation for Each Mode

| Main mode | Slope of the current $i_{L e q}(t)$ for $i$ th mode | Initial current at the start of the $i$ th mode |
| :---: | :--- | :---: |
| $M_{1}$ | $m_{1}=\left(V_{C T 1} d_{1}+V_{C T 2} d_{2}\right) / L_{e q}$ | $i_{L e q}\left(t_{0}\right)=\left(-0.5 d_{1} d_{1}^{\prime} V_{C T 1}-0.5 d_{2} d_{2}^{\prime} V_{C T 2}+\left(d_{2}^{\prime}-\Delta_{\phi}\right) d_{2} V_{C T 2}\right) T_{S W} / L_{e q}$ |
| $\mathrm{M}_{2}$ | $m_{2}=\left(V_{C T 1} d_{1}-V_{C T 2} d_{2}^{\prime}\right) / L_{e q}$ | $i_{L e q}\left(t_{1}\right)=\left(-0.5 d_{1} d_{1}^{\prime} V_{C T 1}+\Delta_{\phi} d_{1} V_{C T 1}+0.5 d_{2} d_{2}^{\prime} V_{C T 2}\right) T_{s w} / L_{e q}$ |
| $\mathrm{M}_{3}$ | $m_{3}=\left(-V_{C T 1} d_{1}^{\prime}-V_{C T 2} d_{2}^{\prime}\right) / L_{e q}$ | $i_{L e q}\left(t_{2}\right)=\left(0.5 d_{1} d_{1}^{\prime} V_{C T 1}+0.5 d_{2} d_{2}^{\prime} V_{C T 2}-\left(d_{1}^{\prime}-\Delta_{\phi}\right) d_{2}^{\prime} V_{C T 2}\right) T_{s w} / L_{e q}$ |
| $\mathrm{M}_{4}$ | $m_{4}=\left(-V_{C T 1} d_{1}^{\prime}+V_{C T 2} d_{2}\right) / L_{e q}$ | $i_{L e q}\left(t_{3}\right)=\left(0.5 d_{1} d_{1}^{\prime} V_{C T 1}-\left(d_{1}-d_{2}^{\prime}+\Delta_{\phi}\right) d_{1}^{\prime} V_{C T 1}-0.5 d_{2} d_{2}^{\prime} V_{C T 2}\right) T_{S W} / L_{e q}$ |

## C. ZVS Condition

ZVS turn-ON requires complete discharging of the output capacitance
( $\mathrm{C}_{\text {oss }}$ ) of the switch turning-ON and complete charging of the $\mathrm{C}_{\mathrm{oss}}$ of the switch turning-OFF within the deadband $t_{\mathrm{db}}$ [32], [33]. $C_{\mathrm{oss}}$ is assumed to be constant, whereas $t_{\mathrm{db}}$ between the gates of the complementary switches is taken as constant for all switches in this article. The deadband $t_{\mathrm{db}}$ between the complimentary switches should be larger than the switching transition time (as discussed in Section II) to achieve full ZVS turn-ON of the switches. Minimum threshold current through the switch, which can charge and discharge the output capacitance of the switches before $t_{\mathrm{db}}$ elapse, is given by the following equation:

$$
\begin{equation*}
i_{\mathrm{ZVS}, \min }=2 C_{\mathrm{oss}} V_{\mathrm{DS}} / t_{\mathrm{db}} \tag{33}
\end{equation*}
$$

where $V_{\mathrm{DS}}$ is the voltage across the switch that is turning OFF. Conditions on current $i_{\text {Leq }}(t)$ required to ensure enough current through the switches at the time of transition for ZVS turn-ON
are obtained using Fig. 4 and are given as follows:

$$
\begin{align*}
& i_{L \mathrm{eq}}\left(t_{2}\right)>\left(I_{\mathrm{in}}-\Delta I_{\mathrm{in}}\right)+2 C_{\mathrm{oss}} V_{C T 1} / t_{\mathrm{db}}\left[\mathrm{ZVS} S_{P 1}\right] \\
& i_{L \mathrm{eq}}\left(t_{0}\right)<\left(I_{\mathrm{in}}+\Delta I_{\mathrm{in}}\right)-2 C_{\mathrm{oss}} V_{C T 1} / t_{\mathrm{db}}\left[\mathrm{ZVS} S_{P 2}\right]  \tag{34b}\\
& i_{L \mathrm{eq}}\left(t_{1}\right)>-\left(I_{o}+\Delta I_{o}\right)+2 C_{\mathrm{oss}} V_{C T 2} / t_{\mathrm{db}}\left[\mathrm{ZVS} S_{S 1}\right]  \tag{34c}\\
& i_{L \mathrm{eq}}\left(t_{3}\right)<-\left(I_{o}-\Delta I_{o}\right)-2 C_{\mathrm{oss}} V_{C T 2} / t_{\mathrm{db}}\left[\mathrm{ZVS} S_{S 2}\right] \tag{34d}
\end{align*}
$$

where $i_{L \text { eq }}\left(t_{i}\right)$ at the time of transition is obtained from Table II. Conditions for ZVS turn-ON of switches $S_{P 2}$ and $S_{S 1}$ are easily achievable as $i_{\text {Leq }}\left(t_{0}\right)<\left(I_{\text {in }}+\Delta I_{\text {in }}\right)$ and $i_{\text {Leq }}\left(t_{1}\right)>$ $-\left(I_{o}+\Delta I_{o}\right)$ are generally satisfied and can be verified using Table II. However, ZVS turn-ON of $S_{P 1}$ and $S_{S 2}$ requires proper selection of $d_{1}, d_{2}$, and $\Delta_{\phi}$. Using (4), (5), (29), (34a), (34c), and Table II, an analytical expression for the ZVS turn-ON conditions


Fig. 8. ZVS turn-ON boundary condition of (a) switch $S_{P 1}$ and (b) switch $S_{S 2}$ as a function of control parameters: duty cycles $\left(d_{1}, d_{2}\right)$ and phase-shift ratio $\Delta_{\phi}$ for varying converter gain, $G$.
of $S_{P 1}$ and $S_{S 2}$ is determined to be

$$
\begin{align*}
& d_{1, \mathrm{ZVS}(P 1)}>\frac{\left(\frac{G}{L_{\mathrm{eq}}}\left(1-\frac{\Delta_{\phi}^{2}}{d_{1}^{\prime} d_{2}^{\prime}}\right)\right)+\frac{4 C_{\mathrm{os}}}{d_{1}^{\prime} \mathrm{tav}_{\mathrm{sw}}}}{\left(\frac{G+1}{L_{\mathrm{eq}}}+\frac{1}{L_{\mathrm{in}}}\right)}  \tag{35a}\\
& d_{2, \mathrm{ZVS}(S 2)}>\frac{\left(\frac{1}{L_{\mathrm{eq}}}\left(1-\frac{\Delta_{\phi}^{2}}{d_{1}^{\prime} d_{2}^{\prime}}\right)\right)+\frac{4 C_{\mathrm{oss}}}{d_{2}^{\prime} t_{\mathrm{db}} T_{\mathrm{sw}}}}{\left(\frac{G+1}{L_{\mathrm{eq}}}+\frac{G}{L_{o}}\right)} \tag{35b}
\end{align*}
$$

where $G\left(=V_{o} / V_{\text {in }}\right)$ is the converter gain. It can be seen from (35) that the ZVS boundary for $S_{P 1}$ is nearly decoupled from $d_{2}$ and for $S_{S 2}$, it is nearly decoupled from $d_{1}$. Fig. 8 shows the plot of the ZVS boundary for $S_{P 1}$ and $S_{S 2}$ for various $G$ values. With the increasing $G$, the ZVS boundary condition of $S_{P 1} d_{1, \mathrm{ZVS}(P 1)}$ decreases, whereas for $S_{S 2}, d_{2, Z V S(S 2)}$ increases [also shown in Fig. 7(a)-(c) as $V_{o}$ is increasing]. It can also be noted from Fig. 8 that increasing the $\Delta_{\phi}$ provides more room for ZVS operation but with an increase in circulating current as discussed previously. An increase in the phase-shift ratio also results in more coupling between ZVS boundary conditions, $d_{1, Z V S(P 1)}$ and $d_{2, Z V S(S 2)}$, as shown in Fig. 8 by the shaded region, making the boundary condition more complex.

## IV. DESIGN CONSIDERATION

## A. Hardware Design

ZVS operation of the PAC-Ćuk converter over a wide output power and voltage range requires proper selection of the passive components based on the control parameter range. The dependence of power transfer, circulating current, and ZVS condition on passive components is evident from (29), (32), and (35), respectively. Hence, proper selection of the components is important and is discussed in detail below.

MOSFET selection: The maximum voltage across $S_{P 1}$ and $S_{P 2}$ is clamped by the auxiliary capacitor $C_{T 1}$, whereas for $S_{S 1}$ and $S_{S 2}$, it is clamped by $C_{T 2}$. Hence, the maximum voltage across these capacitors will dictate the voltage ratings of the switches. For the maximum input voltage and the maximum $d_{1}$, the maximum voltage across $S_{P 1}$ and $S_{P 2}$ can be deduced using (1). Similarly, the maximum voltage across $S_{S 1}$ and $S_{S 2}$ is obtained using (2). Absolute peak currents through the switches $\left(S_{P 1}, S_{P 2}\right)$ and $\left(S_{S 1}, S_{S 2}\right)$ are given by (36) from the turn-OFF current through the switches at the end of the main modes $M_{1}$
and $M_{2}$

$$
\begin{align*}
& i_{P 1, \max }=i_{P 2, \text { max }}=\left|\left(I_{\mathrm{in}, \max }+\Delta I_{\mathrm{in}}\right)-i_{L \mathrm{eq}, \max }\left(t_{0}\right)\right|  \tag{36a}\\
& i_{S 1, \max }=i_{S 2, \max }=\left|\left(I_{o, \text { max }}+\Delta I_{o}\right)-i_{L e \mathrm{eq}, \max }\left(t_{1}\right)\right| \tag{36b}
\end{align*}
$$

Equivalent series inductance, $L_{\text {eq }}$ : Inductance $L_{\text {eq }}$, which is equivalent to $L_{r}+L_{\mathrm{lk}}$, plays a vital role in power transfer and producing the circulating current necessary for the ZVS turn-ON of the switches. Power transfer and the circulating current through the inductor are both inversely proportional to $L_{\text {eq }}$ as given in (29) and (32). The design objective for $L_{\text {eq }}$ is to choose the inductance that satisfies the minimum load requirement for a small constant phase-shift ratio with ZVS turn-ON. Fig. 7(b) and (e) shows the effect of increasing the series inductance, resulting in lower power output and lower mean square circulating current per Watt for the same modulation conditions. Minimum condition for $L_{\mathrm{eq}}$ is given as follows:

$$
\begin{equation*}
L_{\mathrm{eq}}>\frac{V_{\mathrm{in}} V_{o} T_{\mathrm{sw}}}{2 P_{\mathrm{min}}}\left(2 \Delta_{\phi}+d_{1, \mathrm{ZVS}}+d_{2, \mathrm{ZVS}}-1-\frac{\Delta_{\phi}^{2}}{d_{1, \mathrm{ZvS}}^{\prime} d_{2, \mathrm{ZVS}}^{\prime}}\right) \tag{37}
\end{equation*}
$$

where $P_{\text {min }}$ is the minimum required output load and $d_{1, \mathrm{ZVS}}$ and $d_{2, \mathrm{ZVS}}$ are the ZVS boundary constraints on duty cycles given by (35) for a constant $\Delta_{\phi}$.

Input and output inductors, $L_{\text {in }}$ and $L_{o}$ : As in the case of designing a conventional Ćuk converter, input and output inductors are chosen as per ripple requirements. However, higher inductor current ripple over the inductors assists in ZVS operation and is preferred, as evident from ZVS boundary constraints.

Auxiliary capacitors, $C_{T 1}$ and $C_{T 2}$. The auxiliary capacitor $C_{T 1}$ is chosen to make sure that the resonance period of the circuit formed by $C_{T 1}, C_{B 1}, C_{B 2}$, and $L_{\text {eq }}$ is much greater than the maximum duration of the main mode $\left(M_{2}\right)$. Similarly, auxiliary capacitor $C_{T 2}$ should be large enough that the resonance period of the circuit formed by $C_{T 2}, C_{B 1}, C_{B 2}$, and $L_{\mathrm{eq}}$ is much greater than the maximum duration of the main mode $\left(M_{4}\right)$. Conditions (38) and (39) can be used to select the auxiliary capacitor as it ensures a small deviation from the linear analysis presented in this article

$$
\begin{align*}
& \left(1-d_{1, \max }-\Delta_{\phi}\right) T_{\mathrm{sw}} \ll 2 \pi \sqrt{L_{\mathrm{eq}}\left(C_{T 1}\left\|C_{B 1}\right\| C_{B 2}\right)}  \tag{38}\\
& \left(1-d_{2, \max }-\Delta_{\phi}\right) T_{\mathrm{sw}} \ll 2 \pi \sqrt{L_{\mathrm{eq}}\left(C_{T 2}\left\|C_{B 1}\right\| C_{B 2}\right)} \tag{39}
\end{align*}
$$

where $d_{1, \max }$ and $d_{2, \max }$ are the maximum allowable duty cycles, limited by the capacitor and switch voltage ratings.

## B. Control Parameter

The PAC-Ćuk converter has three control parameters, including $d_{1}$ and $d_{2}$ and $\Delta_{\phi}$. An operating condition is achieved using a combination of these three control parameters. The choice of parameters for a given operation can be made based on the required objective. In this article, the objective is to minimizing the circulating current by optimizing the duty cycles for a constant $\Delta_{\phi}$.

Phase-shift ratio, $\Delta_{\phi}$ : The phase between the two duty cycles is responsible for circulating current, which assists in achieving

ZVS turn-ON of the switches. A higher phase-shift ratio $\Delta_{\phi}$ results in higher power flow but also increases circulating current. It also extends the ZVS region, but at the cost of higher circulating current losses, as shown in Fig. 7(d)-(f). In this article, a constant phase-shift ratio is considered for design and operation, where smaller phase-shift results in an overall minimal circulating current for varying duty cycles. As power transfer is dependent upon control parameters (duty cycles $d_{1}$ and $d_{2}$ and $\Delta_{\phi}$ ) and the voltage across the device is dependent on the duty cycle, when the duty cycle cannot be increased due to an allowable voltage constraint, $\Delta_{\phi}$ is increased at the cost of higher circulating current.

Duty cycles, $d_{1}$ and $d_{2}$ : With the phase-shift ratio $\Delta_{\phi}$ held constant, the minimum duty cycles $d_{1, \min }$ and $d_{2, \text { min }}$ are set by ZVS boundary constraint (35), whereas the maximum duty cycles $d_{1, \text { max }}$ and $d_{2, \text { max }}$ are limited by the voltage rating of switches and auxiliary capacitors as given by (1) and (2). Increase in either $d_{1}$ or/and $d_{2}$ also results in higher power transfer, as given by (29). However, an optimal relation between the duty cycles is required to achieve the minimal circulating current for a chosen $\Delta_{\phi}$.

Optimization between duty cycles, $d_{1}$ and $d_{2}$ : According to the Lagrange multiplier method, a common normal to both the contours ( $I_{\mathrm{rms}}^{2} / \mathrm{W}$ and power, $P_{o}$ ) can provide a relationship between duty cycles $d_{1}$ and $d_{2}$, which results in the minimum circulating current $I_{L, \mathrm{RMS}}^{2}$ for a constraint on power $P_{o}$ and is given as follows:

$$
\begin{align*}
\frac{\partial I_{\mathrm{rms}}^{2}}{\partial d_{1}} & =\lambda \frac{\partial P_{o}}{\partial d_{1}}  \tag{40a}\\
\frac{\partial I_{\mathrm{rms}}^{2}}{\partial d_{2}} & =\lambda \frac{\partial P_{o}}{\partial d_{2}}  \tag{40b}\\
P_{o} & =P_{c} \tag{40c}
\end{align*}
$$

where $\lambda$ is the Lagrange multiplier and $P_{c}$ is the constraint for the required output power. Using (29) and (32), the relationship between the duty cycles with the objective of minimal circulating current for a small constant $\Delta_{\phi}$ is found and given as follows:

$$
\begin{equation*}
d_{1} \approx G d_{2} \tag{41}
\end{equation*}
$$

where $G$ is the gain of the converter. This relation can be interrupted in the sense that the PAC-Ćuk converter is a symmetric converter. Gain $G$ creates voltage inequality in the symmetry and is accounted for by (41) through auxiliary capacitor voltages, reducing the circulating current. Also, this relation helps to distribute the voltage stress on the switches. A higher gain results in a smaller duty cycle on secondary main switch $d_{2}$, which, in turn, reduces the voltage stress on the switch.

## V. Hardware Results

A $2-\mathrm{kW}$ rated hardware prototype is designed for the validation of the work outlined in the earlier sections. Table III lists the parameters of the hardware prototype, and a detailed design process of the prototype is given in the Appendix. The TDK EE 65 N 27 cores are used for the input inductor and the output inductor, and the transformer is used for the desired design parameter. The size of the required external inductor $L_{r}$

TABLE III
Design Parameters of the Prototype Converter

| Parameter | Value |
| :---: | :---: |
| $V_{i n}$ | 350 V |
| $V_{o}$ | $245-455 \mathrm{~V}$ |
| $L_{l k}$ | $170 \mu \mathrm{H}$ |
| $L_{r}$ | $30 \mu \mathrm{H}$ |
| $L_{i n}, L_{o}$ | 1 mH |
| $L_{m}$ | 1.92 mH |
| $C_{T 1}, C_{T 1}$ | $3.8 \mu \mathrm{~F}$ |
| $C_{B 1}, C_{B 1}$ | $3.8 \mu \mathrm{~F}$ |
| $C_{i n}, C_{o}$ | $2 \mu \mathrm{~F}$ |
| $P_{1}, P_{2}, S_{1}, S_{2}$ | UF 3 C 120040 K 4 S |
| Switching frequency $f_{s w}$ | 40 kHz |
| $d_{1, \text { max }}$, and $d_{2, \text { max }}$ at $G=1$ | 0.6 |




Fig. 9. Comparison of voltage and current stresses on switches for the $R C$ snubber ( $R=50 \Omega$ and $C=2.2 \mathrm{nF}$ )-based isolated Cuk converter with the proposed PAC-Ćuk converter when $V_{\mathrm{in}}=V_{o}=350 \mathrm{~V}$.
is reduced by adopting nonconcentric primary and secondary windings for the transformer.

A comparison of peak voltage and peak current stresses on the switches for the designed prototype is shown in Fig. 9 using simulation. Converter gain of $G=1$ is used for which the nominal voltage across the primary- and secondary-side switches is the same due to symmetry. A comparison of the proposed modulation scheme for the PAC-Ćuk converter and the hard-switched Ćuk converter with an $R C$ snubber is also shown in the figure with variations in the output power. A separate transformer with the same magnetic core and number of turns as used for the PAC-Ćuk converter was built for the hard-switched converter to determine the leakage inductance. The secondary winding is sandwiched between the primary winding to attain a low leakage inductance of $L_{\mathrm{lk}}=4.5 \mu \mathrm{H}$. The $R C$ snubber are tuned to limit the $v_{\text {ds }}$ overshoot to the maximum allowed voltage. For the proposed optimized modulation using duty cycles to control the output power, the voltage stress increases whereas the current stress decreases for the increase in $\Delta_{\phi}$, as shown in the figure. In comparison to the $R C$-snubber-based isolated Ćuk converter, the peak voltage and current stresses are observed to be lower for the proposed modulation on the PAC-Ćuk converter.


Fig. 10. Photograph of the (a) 2-kW hardware prototype and (b) test bench.


Fig. 11. Operating region for minimum circulating current condition ( $d_{1}=G d_{2}$ ) of the designed hardware with $\Delta_{\phi}=0.05$.

Fig. 10 shows the photograph of the hardware prototype and the test bench. A digital power meter, WT230 from Yokogama, is used to measure the efficiency of the converter. A digital controller, TMS320F28379D from Texas Instruments, is used to generate the required PWM signal. An electronic load from NHR research is used in the CV mode to operate the converter at the output power for the desired converter gain. The output power flow is controlled using the duty cycles $d_{1}$ and $d_{2}$, where $d_{1}=G d_{2}$.

Fig. 11 shows the ideal allowed region of operation of the designed prototype for minimum circulating current constraint, $d_{1}=G d_{2}$ obtained from (41). The ZVS constraint for $S_{P 1}$ and $S_{S 2}$ limits the minimum output power set by (37), whereas the voltage rating limit of the components defined by $V_{C T 1, \max }$ and $V_{C T 2, \max }$ limits the maximum output power.


Fig. 12. Experimental verification of ZVS turn-ON of (a) $S_{P 1}$ and $S_{S 2}$, and (b) $S_{P 2}$ and $S_{S 1}$, for point 1: Gain $G=0.7$ and $P_{\text {in }}=210 \mathrm{~W}$.

The ZVS operation of all the active switches of the designed hardware prototype is shown for three operating points as marked in Fig. 11. For operating point 1, as shown in Fig. 12, switches $S_{P 1}$ and $S_{S 2}$ are losing ZVS turn-ON, which is in agreement with the ZVS constrain shown in Fig. 11. For operating points 2 and 3 (see Figs. 13 and 14, respectively), ZVS turn-on of all switches can be observed as the drain-source voltage, $v_{\mathrm{ds}}$, falls to 0 V before the gate, $v_{\mathrm{gs}}$, is applied, confirming the ZVS turn-ON of the switches. The drain-to-source voltages of devices are also marked in the figures and are observed to satisfy the auxiliary capacitor voltages given by (1) and (2).

The power transfer relation given by (29) and the rms of series inductor current $I_{L, \text { rms }}$ given by the square root of (32) are compared with the experimental data shown in Fig. 15 for validation for unity-gain operation. The maximum percentage error on output power is $2.5 \%$, whereas the maximum error for $I_{L, \mathrm{rms}}$ is $7.5 \%$. As the analysis for power transfer and circulating current was derived for ideal passive components, the experimental data are within reasonable error. The discrepancy can be accounted for by parasitic resistance of the components and the variation of series inductance with different bias currents.

The prototype efficiency under different gains is shown in Fig. 16. The proposed modulation is used to control the output power flow by increasing $d_{1}$ and $d_{2}$ while keeping $\Delta_{\phi}$ at 0.05 . The duty cycle of the secondary-side switch is defined by (41) for the minimum circulating current. The efficiency for a gain of 1.3 is observed to be higher for higher loads owing to smaller conduction losses in comparison to the power transferred. The measured peak efficiency is $97.8 \%$ when gain $G=0.7$, whereas the overall efficiency for the designed prototype converter is above $96 \%$ for $20 \%$ to full load over a wide gain (0.7-1.3).


Fig. 13. Experimental verification of ZVS turn-ON of (a) $S_{P 1}$ and $S_{S 2}$, and (b) $S_{P 2}$ and $S_{S 1}$, for point 2: Gain $G=1.0$ and $P_{\text {in }}=2064 \mathrm{~W}$.

(a)

(b)

Fig. 14. Experimental verification of ZVS turn-ON of (a) $S_{P 1}$ and $S_{S 2}$, and (b) $S_{P 2}$ and $S_{S 1}$, for point 3: Gain $G=1.3$ and $P_{\text {in }}=2035 \mathrm{~W}$.

The converter was not operated till 2 kW for lower gain due to the saturation limit of the output inductor. Fig. 17(a) shows the estimated loss distribution of the prototype at an output power of 2 kW and at unity gain, whereas Fig. 17(b) shows the thermal image of the switches, which are located at the


Fig. 15. Comparison of calculated and experimental data for (a) output power $P_{o}$, (b) series inductor current, $I_{L, \text { rms }}$, using the proposed optimized modulation ( $d_{1}=G d_{2}$ ) for $\Delta_{\phi}=0.05$ and unity gain $\left(V_{\text {in }}=V_{o}=350 \mathrm{~V}\right)$.


Fig. 16. Measured efficiency versus output power for various gains with constant input voltage $V_{\text {in }}=350 \mathrm{~V}$ and $\Delta_{\phi}=0.05$
bottom of the converter. Due to ZVS turn-ON, the switching losses are significantly reduced. Low losses on the switches as shown in Fig. 17(a) enables the use of low form factor heat-sink, resulting in the switch temperature rise to $47^{\circ} \mathrm{C}$. For the designed magnetics, more than half of the losses are incurred in $L_{r}$ and $T_{1}$, resulting in hotspots of $78{ }^{\circ} \mathrm{C}$ and $62^{\circ} \mathrm{C}$, respectively, at rated power.

The proposed modulation is optimized to minimize the circulating current through $L_{\text {eq }}$ for constant output power. The power transfer given by (29) for $d_{1}+d_{2}=k$ becomes nearly independent from the duties for a constant, $k$. The $d_{1}$ and $d_{2}$ at which $I_{L, \text { rms }}$ is minimum with $d_{1}+d_{2}=k$ are the optimized duties for that output power. In Fig. 18(a), three different output power cases with unity gain are presented, where circulating inductor current $I_{L, \text { rms }}$ normalized by output power is measured against $d_{1},\left(d_{2}=k-d_{1}\right)$ for different $k$ values. The experimental data prove that the proposed modulation ( $d_{1}=G d_{2}$ ) operates the converter with minimal circulating current for a wide power range. Fig. 18(b) shows the efficiency comparison of the conventional modulation (as used in [23]-[25] and [27]) and the proposed modulation over the output power. ZVS is ensured in both the modulation cases to provide a fair comparison. As discussed earlier, the conventional modulation $\left(d_{2}=1-d_{1}\right)$


Fig. 17. 2-kW unity gain operation of the converter. (a) Projected loss distribution. (b) Thermal image of the switches.


Fig. 18. Experimental data showing (a) circulating inductor current $I_{L, \text { rms }}$ normalized by output power for $d_{1}+d_{2}=k$ to validate the proposed optimized modulation ( $d_{1}=G d_{2}$ ). (b) Efficiency comparison between the proposed modulation and the conventional modulation $\left(d_{1}=1-d_{2}\right)$ of the PAC-Ćuk converter.


Fig. 19. Experimental results for (a) comparison of forward and backward power flow and efficiency for $\Delta_{\phi}=0.05$ and unity gain and (b) transition from backward to forward power flow by changing $\Delta_{\phi}$ reference from backward to forward with a rate limiter. Orange trace is the current entrying the converter, $I_{\text {in }}$, through the input port, light blue is the voltage at the input port, $V_{\mathrm{in}}$, and blue trace is the digital to analog converter (DAC) ouput of digital signal processor (DSP) indicating PWM phase-shift.
does not provide output power control through the duties. Hence, $\Delta_{\phi}$ varies for the conventional modulation. The proposed modulation offers better efficiency than the conventional modulation, as shown in the figure. The difference is more prominent for low- and full-load conditions. The efficiency for conventional modulation drops rapidly near full-load condition due to high $\Delta_{\phi}$, which results in a steep rise in circulating current.

The PAC-Cuk converter is symmetric, and the power flow can be reversed by generating $\Delta_{\phi}$ referred to the power delivery side of the main switch. By generating $\Delta_{\phi}=0.05$ for both forward and backward power flows, the bidirectional efficiency plot of the converter is obtained as shown in Fig. 19(a) for unity gain. The efficiency plot is near symmetric along the $y$-axis due to the converter symmetry. In Fig. 19(b), the converter transition from backward to forward is shown at derated input voltage of 100 V using unidirectional sources and loads. $\Delta_{\phi}$ is gradually shifted from backward to forward, as shown by the blue trace in the figure. During backward flow, current $I_{\text {in }}$ is negative at -1.21 A and gradually increases to 1.09 A at the end of the power reversal transition period. The voltage across the switches remains stable during the transition while maintaining ZVS turnON as shown in the zoomed snippet at the zero-crossing of the current, showcasing smooth power reversal transition.

## VI. CONCLUSION

This article proposes a novel modulation scheme for an isolated dc/dc PAC-Ćuk converter for a wide voltage range application. Using the leakage of the isolation transformer, the proposed scheme provides three control parameters, i.e., primary-side main switch duty cycle $d_{1}$, secondary-side main switch duty cycle $d_{2}$, and the phase-shift ratio between the two switches, $\Delta_{\phi}$. A new model of PAC-Ćuk to find the output power transfer, circulating current, and ZVS region of the converter as a function of these control parameters was derived and validated through experimental data. The optimality between duty cycles to minimize the circulating current through the series inductor is also discussed and verified through experiment. As ZVS turn-ON is essential to achieve high efficiency on the converter, ZVS conditions were analyzed and experimentally validated. From the analysis, it is observed that the optimality between the duty cycles and the ZVS constraints is simple to compute for the proposed converter. Finally, a $2-\mathrm{kW}$ prototype with an input voltage of 350 V was demonstrated over wide load conditions for an output voltage range of $245-455 \mathrm{~V}$. The converter achieved a peak efficiency of $97.8 \%$ for an output voltage of 245 V while maintaining a flat efficiency curve for $20 \%$ or more of the rated power operation.

## APPENDIX <br> Design Process of the Prototype

Required design specification for the prototype:

$$
\begin{aligned}
P_{\max } & =2 \mathrm{~kW}, P_{\min }=400 \mathrm{~W}, V_{\mathrm{in}}=350 \mathrm{~V}, f_{\mathrm{sw}} \\
& =40 \mathrm{kHz}, t_{\mathrm{db}}=0.03 T_{\mathrm{sw}}, \text { and } G=1
\end{aligned}
$$

Using (4) and (5), the input and output inductors are selected at 1 mH for $50 \%$ ripple condition in a full-load operation. As the input voltage is 350 V and the maximum output voltage is 455 V for gain of $1.3,1200 \mathrm{~V}$-rated mosfets are chosen for switches $S_{P 1}, S_{P 2}, S_{S 1}$, and $S_{S 2}$. UF3C120040K4S is used as the choice of MOSFET, which has $C_{\text {oss }}=280 \mathrm{pF}$. The minimum duty cycles with ZVS $d_{1, \mathrm{ZvS}}$ and $d_{2, \mathrm{ZvS}}$ are dependent on $L_{\mathrm{eq}}$, and iterations using (35) and (37) are used to select $L_{\text {eq }}$ for the required minimum output power with ZVS for $\Delta_{\phi}=0.05$. $L_{\text {eq }}$ $=200 \mu \mathrm{H}$ is obtained, satisfying the minimum output power under the ZVS constraint with $d_{1 . \mathrm{ZvS}}=d_{2 . \mathrm{ZvS}}=0.4705$. The maximum allowable duty cycle is dictated by the voltage rating of the device and the auxiliary capacitors as given by (1) and (2). Setting the allowable voltage to 950 V , maximum duty cycles $d_{1, \text { max }}$ and $d_{2, \text { max }}$ are equal to 0.63 . Using (38) and (39), assuming $C_{B 1}=C_{B 2}=C_{T 1}=C_{T 2}=C_{x}$, and taking the maximum duration of mode to be 8 times the resonance period, we have, $C_{x, \text { cal }}=3.43 \mu \mathrm{~F}$. For these capacitors, film capacitor C4AQNLW4380M34J of $3.8 \mu \mathrm{~F}$ is used, which has a rated voltage of 1 kV .

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